# Innovation, R&D spillovers, and the variety and concentration of local production structure

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## Introduction

- Stylised fact: Innovation is more geographically concentrated than production.
- Explanation: localised knowledge spillovers induce agglomeration and result to higher levels of innovation.
- Glaeser et al. (1992): Is this due to spillovers within or across industries? How does local production structure affect innovation?

## Which local factors enhance innovation?

		Diversity
Concentration		X
	MAR externalities	
Competition	Porter externalities	Jacobs externalities

## What is the rationale behind these hypotheses?

- The theoretical foundation of the hypotheses is vague.
- Empirical results have been very mixed (Beaudry & Schiffauerova 2009, de Groot et al. 2009)
  - Model specification, measurement and methodological issues.
- Research questions:
  - How does variety and concentration affect firms' innovation incentives and, subsequently, effective R&D and output?
  - Under what conditions would we expect these hypotheses to hold?

## A very concise literature review

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- Papers on spillovers between vertically related firms (Atallah 2002, Ishii 2004)
- Steurs (1995) seems to be the only paper that studies simultaneously both intra-industry and inter-industry spillovers between segmented markets
  - 2 industries that have 2 firms each
  - Inter-industry spillovers always increase effective R&D but they also reinforce the disincentive effect of intra-industry spillovers

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- Markets are identical and segmented with inverse demand  $P_j = a Q_j$ , where  $Q_j = \sum_{i=1}^n q_{ij}, \ \forall j \in m$ .
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$$X_{ij} = x_{ij} + \beta \sum_{k \neq i} x_{kj} + \sigma \sum_{l \neq j} \sum_{i \neq j} x_{il}, \ \beta, \sigma \in [0, 1],$$

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- R&D cost is given by  $\frac{1}{2}\gamma x_{ij}^2$ , where  $\gamma$  is an inverse measure of R&D efficiency.
- $\pi_{ij} = (a c + X_{ij} Q_j)q_{ij} \frac{1}{2}\gamma x_{ij}^2$ ,  $i \in n, j \in m$ .

- Stage 1: Firms simultaneously choose their R&D outputs,  $x_{ij}$ ,  $i \in n, j \in m$ .
- Stage 2: Firms simultaneously choose their final good outputs,  $q_{ij}$ ,  $i \in n, j \in m$  (Cournot competition).

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- Solve by backward induction for symmetric equilibria:

$$q_{ij}^* = \frac{a - c + X_{ij} - \sum_{k \neq i} X_{kj}}{n+1}, \ Q_j = \frac{n(a-c) + \sum_{i=1}^n X_{ij}}{n+1}.$$

$$x^* = \frac{2(a-c)(n-(n-1)\beta)}{\gamma(n+1)^2 - 2(n-(n-1)\beta)(n\sigma(m-1) + (n-1)\beta + 1)}.$$

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- Effective R&D:  $X = (n\sigma(m-1) + (n-1)\beta + 1)x^*$ .
- Equilibrium output levels:  $q^* = \frac{a-c+X}{n+1}$  and  $Q = nq^*$ .

## Proposition

Effective R&D always increases with inter-industry spillover rate,  $\sigma$ , whereas the intra-industry spillover rate that maximises effective R&D is given by  $\beta^* = \max\{\frac{1}{2} \frac{n-1-n\sigma(m-1)}{n-1}, 0\}$ .

• Effective R&D is maximised for  $\beta=0, \sigma=1$ , but this may not be a likely situation.

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#### Proposition

If intra- and inter-industry spillover rates are equal,  $\beta = \sigma = \phi$ , then the common spillover rate that maximises effective R&D is given by

$$\phi^* = \frac{1}{2} \frac{n^2 m - 2n + 1}{n^2 m - nm - n + 1} \in \left[\frac{1}{2}, 1\right)$$
, with  $\frac{\partial \phi^*}{\partial m} > 0$ ,  $\frac{\partial \phi^*}{\partial n} < 0$ .

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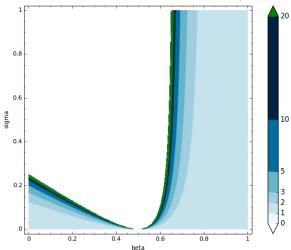
## Proposition

If 
$$3\beta\sigma m + 4\beta^2 - 3\beta\sigma - 2\sigma m - 4\beta + 2\sigma + 1 \leq 0$$
, then effective R&D is always increasing in n. Otherwise, effective R&D is maximised for  $n^* = \frac{\beta\sigma m + 4\beta^2 - \beta\sigma - 4\beta + 1}{3\beta\sigma m + 4\beta^2 - 3\beta\sigma - 2\sigma m - 4\beta + 2\sigma + 1}$  firms.

- The effect of *n* is conditional on  $\beta$ ,  $\sigma$  and *m*.
- For example, a finite  $n^*$  if  $\beta \geq 2/3$ .

## Optimal n

The number of firms that maximises X, when m = 3.



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## Corollary

In the absence of inter-industry R&D spillovers or holding them constant, monopoly maximises effective R&D, expect when  $\beta=\frac{1}{2}$ , in which case the number of firms has no effect.

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#### Corollary

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- However, effective R&D may not always be the relevant performance measure.
- Typical measures: Economic growth (employment, wages),
  Productivity (output, value added), Innovation (patents, expenditures) (Beaudry & Schiffauerova 2009).

# Comparative statics of total industry output

## Proposition

Total industry output is increasing in m and  $\sigma$ , as well as in  $\beta$  when  $\beta \leq \max\{\frac{1}{2}\frac{n-1-n\sigma(m-1)}{n-1}, 0\}$ .

• This is simply because output is increasing in effective R&D.

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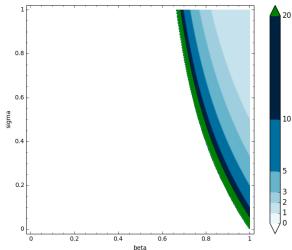
## Proposition

Total industry output is increasing in n if  $4\beta\sigma m + 6\beta^2 - 4\beta\sigma - 2\sigma m - 6\beta + 2\sigma + 2 - \gamma \leq 0. \ \ \text{Otherwise, total}$  industry output is maximised for  $n^* = \frac{2(2\beta^2 - 2\beta + \gamma)}{4\beta\sigma m + 6\beta^2 - 4\beta\sigma - 2\sigma m - 6\beta + 2\sigma + 2 - \gamma}$  firms.

• The effect of n is now also conditional  $\gamma$ .

## Optimal n

The number of firms that maximises Q, when m=3,  $\gamma=2$ .



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• Industry output can be increasing in *n* even when effective R&D is not.

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In the absence of inter-industry R&D spillovers or holding them constant, total industry output is always increasing in n when  $\gamma \geq 6\beta^2 - 6\beta + 2$  and never maximised by monopoly.

• The choice of the performance measure matters!

- Effective R&D and industry output are always increasing with variety (Jacobs externalities).
- However, the effect of competition depends on both spillover rates, variety, and, in the case of output, R&D efficiency.

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- However, the effect of competition depends on both spillover rates, variety, and, in the case of output, R&D efficiency.
- If variety is low, concentration typically increases effective R&D (MAR externalities).
- If variety is low, competition typically increases industry output (Porter externalities).

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- Dependent variable: Q and X, for example, may move in different directions.
- Independent variables: average local concentration vs. industry specific concentration.
- Which industries are related (Frenken et al. 2007)?
- The use of relative measures makes comparison difficult and has also affected the results (de Groot et al. 2009).
- A standard model, but does it capture the essence of these hypotheses (e.g. absorptive capacity, firm survival, creativity)?

## THANK YOU!